

2023 RELEASED FREE RESPONSE SOLUTIONS – MR. CALCULUS

2023 AB #2  
(calculator-active)

(a)

Stephen changes direction when  $v(t) = 0$  and  $v(t)$  changes signs.

When  $0 < t < 90$ ,  $v(t) = 0$  when  $t = 56$  and  $v(t)$  changes from positive to negative there.

Hence, Stephen changes direction when  $t = 56$ .

(b)

$$a(60) = v'(60) = \boxed{-0.0360162389 \frac{m}{\text{sec}}}{\text{sec}} \text{ or } -0.036 \frac{m}{\text{sec}}{\text{sec}}$$

$$v(60) = -0.1595124013$$

Stephen is **speeding up** at  $t = 60$  because his velocity and acceleration are both negative then.

(c)

The displacement or distance between the position at  $t = 20$  and  $t = 80$  is

$$\int_{20}^{80} v(t) dt = \boxed{23.38399745m} \text{ or } 23.383 \text{ or } 23.384$$

(d)

The total distance traveled from  $t = 0$  to  $t = 90$  is

$$\int_0^{90} |v(t)| dt = \boxed{62.16421624m} \text{ or } 62.164$$